

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
TOTAL	



General Certificate of Education
Advanced Level Examination
January 2012

Mathematics

MFP4

Unit Further Pure 4

Friday 27 January 2012 9.00 am to 10.30 am

For this paper you must have:

- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed

- 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer the questions in the spaces provided. Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



J A N 1 2 M F P 4 0 1

Answer **all** questions in the spaces provided.

1 The vectors **a** and **b** are such that $\mathbf{a} \cdot \mathbf{b} = 21$, $|\mathbf{a}| = 5\sqrt{2}$ and $|\mathbf{b}| = 3$.

Determine the exact value of $|\mathbf{a} \times \mathbf{b}|$. (5 marks)

QUESTION
PART
REFERENCE



7 The plane transformation T is a rotation through θ radians anticlockwise about O , and maps points (x, y) onto image points (X, Y) such that

$$\begin{bmatrix} X \\ Y \end{bmatrix} = \begin{bmatrix} c & -s \\ s & c \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

where $c = \cos \theta$ and $s = \sin \theta$.

(a) Write down the inverse of the matrix $\begin{bmatrix} c & -s \\ s & c \end{bmatrix}$ and hence show that

$$x = cX + sY \quad \text{and} \quad y = -sX + cY \quad (3 \text{ marks})$$

(b) The curve C has equation $x^2 - 6xy - 7y^2 = 8$.

The image of C under T is the curve C' with equation $pX^2 + qXY + rY^2 = 8$.

(i) Use the results of part **(a)** to show that

$$q = 6s^2 + 16sc - 6c^2$$

and express p and r similarly in terms of c and s . (4 marks)

(ii) Given that θ is an acute angle, find the values of c and s for which $q = 0$ and hence in this case express the equation of C' in the form

$$\frac{X^2}{a^2} - \frac{Y^2}{b^2} = 1 \quad (8 \text{ marks})$$

(iii) Hence explain why C is a hyperbola. (1 mark)

QUESTION
PART
REFERENCE

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QUESTION
PART
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END OF QUESTIONS

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